

## HADRONIC CENTRALITY DEPENDENCE IN NUCLEAR COLLISIONS

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The kaon number density in nucleus+nucleus and p+p reactions is investigated for the first time as a function of the initial energy density  $\epsilon$  and is found to exhibit a discontinuity around  $\epsilon=1.3$  GeV/fm<sup>3</sup>. This suggests a higher degree of chemical equilibrium for  $\epsilon > 1.3$  GeV/fm<sup>3</sup>. It can also be interpreted as reflection of the same discontinuity, appearing in the chemical freeze out temperature (T) as a function of  $\epsilon$ . The  $N^{\alpha \sim 1}$  dependence of (u,d,s) hadrons, with N the number of participating nucleons, also indicates a high degree of chemical equilibrium and T saturation, reached at  $\epsilon > 1.3$  GeV/fm<sup>3</sup>. Assuming that the intermediate mass region (IMR) dimuon enhancement seen by NA50 is due to open charm ( $D\bar{D}$ ), the following observation can be made: a) Charm is not equilibrated. b)  $J/\Psi/D\bar{D}$  suppression -unlike  $J/\Psi/DY$ - appears also in S+A collisions, above  $\epsilon \sim 1$  GeV/fm<sup>3</sup>. c) Both charm and strangeness show a discontinuity near the same  $\epsilon$ . d)  $J/\Psi$  could be formed mainly through  $c\bar{c}$  coalescence. e) The enhancement factors of hadrons with u,d,s,c quarks may be connected in a simple way to the mass gain of these particles if they are produced out of a quark gluon plasma (QGP). We discuss these results as possible evidence for the QCD phase transition occurring near  $\epsilon \sim 1.3$  GeV/fm<sup>3</sup>.

## 1 Introduction

The quark-gluon plasma phase transition predicted by QCD <sup>3</sup> may occur and manifest itself in ultrarelativistic nuclear collisions through discontinuities in the initial energy density ( $\epsilon_i$ ) dependence of relevant observables. A major example of a discontinuity is seen in the  $J/\Psi/DY$  <sup>4</sup> discussed e.g. in <sup>5,6</sup>. We investigate for the first time the dependence of strangeness production, in particular of kaons, on the initial energy density  $\epsilon_i$  <sup>11,10</sup>. The degree of equilibrium achieved in nuclear collisions has been intensively studied comparing hadron ratios and densities to models (see e.g. <sup>6,7,8,9</sup>). We investigate here if chemical equilibrium is achieved, examining another aspect of equilibrium states, namely the volume (V) independence of hadron densities ( $\rho$ ).<sup>a</sup>

## 2 Results and discussion

The kaon density ( $\rho_K=(K \text{ per collision})/V$ ) at the thermal freeze out in nuclear reactions, investigated as a function of the initial energy

density  $\epsilon_i$  (figure 1) (see <sup>10</sup> for calculation details), exhibits a dramatic changeover around  $\epsilon=1.3$  GeV/fm<sup>3</sup>, saturating for higher  $\epsilon$  values, while it is falling below. The syst. error on  $\epsilon_i$  is estimated to be  $\sim 30\%$ . It is assumed that the number of nucleons participating in the collision (N) is proportional to the volume of the particle source at the thermal freeze out <sup>10</sup>. The new results from Si+Au at 14.6 A GeV and p+p at 158 A GeV shown in figure 1, which are not included in <sup>10</sup>, have been estimated using data from <sup>12</sup> and methods described in <sup>10</sup>. Furthermore,  $\rho_K$  rises with N respectively with V below  $\epsilon=1.3$  GeV/fm<sup>3</sup> while it does not depend on N respectively on V above  $\epsilon=1.3$  GeV/fm<sup>3</sup>. To illustrate this, two values of V are noted on figure 1. The changes of  $K^\pm$  and  $\pi^\pm$  with N within the Pb+Pb system, have been first realized in <sup>13</sup>. A similar behaviour as the one seen in figure 1, can be inferred for pions as well as for the  $K/\pi$  ratio (S.K. work in progress).

The  $N^\alpha$  exponent of hadrons with (u,d,s) quarks above  $\epsilon=1.3$  GeV/fm<sup>3</sup>, do not depend on the particle mass (figure 3). At  $\epsilon > 1.3$  GeV/fm<sup>3</sup>  $\alpha$  is near to one, as expected in case of a chemically equilibrated state, assuming

<sup>a</sup>Results of the NA52 experiment shown in this talk can be found in <sup>1,2</sup>.

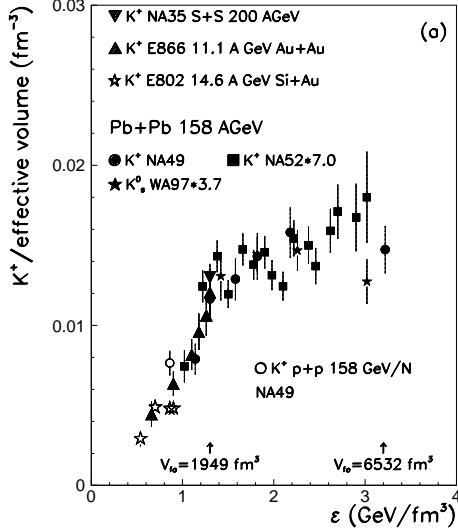


Figure 1. Initial energy density ( $\epsilon$ ) dependence of the  $K^+$  multiplicity over the effective volume of the particle source at thermal freeze out <sup>10</sup>.

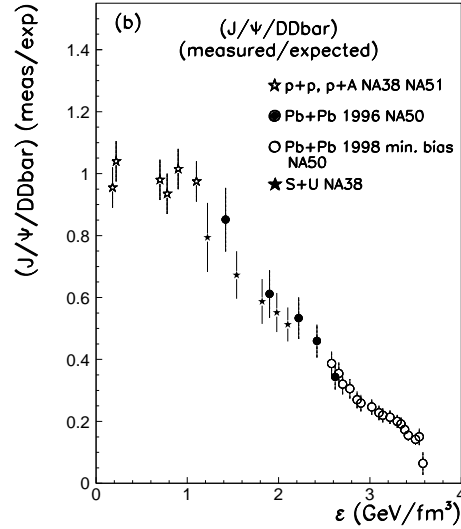


Figure 2. Initial energy density ( $\epsilon$ ) dependence of the  $J/\psi/DD̄$  (measured/expected) ratio <sup>10</sup>.

$N \sim V$ . The deviations seen in  $\phi$ ,  $\pi^0$  and  $\bar{p}$  may be due to the transverse momentum acceptance. Therefore, figure 3 supports the assumption of a high degree of chemical equilibrium reached above  $\epsilon=1.3$  GeV/fm<sup>3</sup>, among hadrons with u,d,s quarks. The  $N^\alpha$  exponent of kaons is found to depend strongly on  $\sqrt{s}$  for kaons (figure 4). Therefore, below  $\epsilon=1.3$  GeV/fm<sup>3</sup>,  $\rho_k$  (figure 1 and figure 4),  $\rho_\pi$  and the  $K/\pi$  ratio, show an increase with increasing  $N$  respectively with  $V$ .

Figures 1, 3 and 4 can be interpreted in two ways. Firstly, kaons may achieve a higher degree of chemical equilibrium only for  $\epsilon > 1.3$  GeV/fm<sup>3</sup>, and may not be fully equilibrated below <sup>10</sup>. The equilibration of strangeness is expected in a QGP and its observation at  $\epsilon \sim 1.3$  GeV/fm<sup>3</sup> could therefore be a sign of a transition to QGP. In this case, it is a transition from a non equilibrated hadron gas to an equilibrated QGP. It is therefore not a well defined phase transition in the thermodynamic sense.

Secondly, kaons can be in fact chemically equilibrated also below  $\epsilon=1.3$  GeV/fm<sup>3</sup>, and

the change respectively the constancy of  $\rho_K$  with  $V_{fo}$  and  $\epsilon_i$  observed in figure 1, can be a result of the increase of the freeze out temperature with  $\epsilon_i$  below  $\epsilon=1.3$  GeV/fm<sup>3</sup>, respectively of the stability of  $T_{fo}$  above  $1.3$  GeV/fm<sup>3</sup>. This dependence of  $T_{fo}$  on  $\epsilon_i$ , namely rising until it reaches a critical  $T_c$  value and saturating above for all reactions, would strongly support the QCD phase transition appearing at  $\epsilon \sim 1.3$  GeV/fm<sup>3</sup>. This interpretation fully agrees with thermal models which suggest that particle ratios at freeze out are compatible with thermalization even in A+A collisions at 1 A GeV <sup>7</sup>. However the first interpretation is not in gross disagreement with <sup>7</sup>, because there the thermal model description is modified (introducing e.g.  $\rho_k \sim V$ ) in order to describe the data at 1 A GeV.

Furthermore, the correct interpretation can be corroborated by further investigations discussed in the following. The nonzero baryochemical potential ( $\mu_B$ ), which in the reactions shown in figure 1, happens to change with  $\epsilon_i$ , makes the interpretation of figure 1 difficult. Therefore, it appears that the dependence of the temperature at chemical

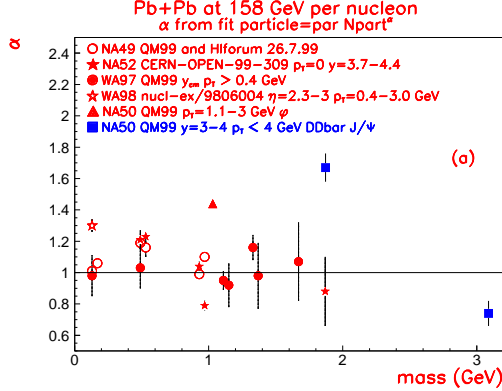


Figure 3. The parameter  $\alpha$ , resulting from the  $N^\alpha$  fit to hadron yields shown as a function of the mass of the particles in the region  $\epsilon > 1.3 \text{ GeV/fm}^3$  at SPS.  $N$  is the number of participating nucleons.

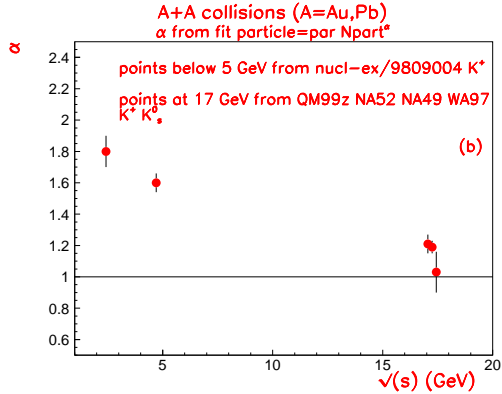


Figure 4. The parameter  $\alpha$ , resulting from the  $N^\alpha$  fit to hadron yields shown as a function of  $\sqrt{s}$  for kaons.  $N$  is the number of participating nucleons.

freeze out extrapolated to  $\mu_b=0$ , on  $\epsilon_i$ , would help to identify and prove the QCD phase transition. A rising and then a for ever saturating freeze out temperature above  $\epsilon > 1.3 \text{ GeV/fm}^3$  is a strong argument that the QCD phase transition occurs at this  $\epsilon$ , and figure 1 is a direct consequence of it.

The question if the QCD phase transition appears at the critical  $\epsilon_i$  in any volume, or if there is additionally a critical initial volume of the particle source above which the transition takes place, can be answered comparing QGP signatures in systems with different volumes but the same  $\epsilon_i$ . For example comparing  $p+p$ ,  $e^+e^-$  etc collisions to heavy ion col-

lisions e.g. at the same  $\epsilon$ . This is not yet done for the signature of the  $J/\Psi$  suppression and it has to be clarified e.g. using Tevatron data<sup>10</sup>. For the signature of strangeness enhancement it is suggested by figure 1 in<sup>8</sup> that there is indeed a critical initial volume, only above which strangeness is enhanced over  $p + \bar{p}$  at the same  $\epsilon_i$ . This conclusion follows, if we assume that Tevatron reaches at least  $\epsilon_i$  values similar to SPS A+A collisions<sup>14</sup> and if figure 1 in<sup>8</sup> is not biased by the model calculation<sup>8</sup>.

If strangeness is indeed not equilibrated at  $\epsilon < 1.3 \text{ GeV/fm}^3$ , this may explain the decrease of the double ratio  $(K/\pi)(A+A/p+p)$  with increasing  $\sqrt{s}$ . In particular, a larger strangeness annihilation is enforced by equilibrium at SPS reducing the strange particle yield. However the assumption of non equilibrium of  $s\bar{s}$  at low  $\epsilon$  is not necessary here, since the above observation can be possibly traced back to e.g. the variation of  $\mu_B(A+A)/\mu_B(p+p)$  with  $\sqrt{s}$  in A+A collisions. Furthermore, in the context of QGP formation, it seems irrelevant to discuss e.g.  $s\bar{s}$  enhancement in A+B over p+p collisions in a nonequilibrium situation. It is the very establishment of equilibrium in the (u,d,s) sector, which can reveal informations on QGP.

The kaon number densities in p+p and A+B collisions in figure 1 are similar, when compared at the same  $\epsilon_i$ . See also<sup>15</sup> for a discussion of universality of pion phase space densities.

Our prediction for the  $N$  dependence of hadrons at RHIC and LHC is the  $N^1$  thermal limit, as long as hadron yields are dominated by low transverse momentum particles. Furthermore, if the changeover of  $\rho_k$  at  $\epsilon = 1.3 \text{ GeV/fm}^3$  shown in figure 1 is due to the QCD phase transition, we predict for RHIC and LHC the same total strangeness (or kaon) number density and the same freeze out temperature, -after correction for the

$\mu_B$  dependence-, as for  $\epsilon = 1.3-3.0$  GeV/fm<sup>3</sup>. If this change is however due to the onset of equilibrium in a hadronic gas, and the QCD phase transition takes place at higher  $\epsilon$ , it may manifest itself through a second changeover of hadron number densities, ratios and freeze out temperatures -after correction for the different  $\mu_B$ - e.g. in RHIC above  $\epsilon \sim 3$  GeV/fm<sup>3</sup>.

Assuming that the IMR dimuon enhancement seen by NA50 is due to open charm, the following observations can be made: a) open charm appears not to be equilibrated ( $\alpha = 1.7$ ) (figure 3)<sup>10</sup>. b) The  $J/\Psi/D\bar{D}$  ratio deviates from p+p and p+A data also in S+U collisions (figure 2), above  $\epsilon \sim 1$  GeV/fm<sup>3</sup>. c) It therefore appears that both charm and strangeness show a discontinuity near the same  $\epsilon \sim 1$  GeV/fm<sup>3</sup><sup>10</sup>, similar to the critical  $\epsilon_c \sim 1-2$  GeV/fm<sup>3</sup> predicted by QCD<sup>3,5</sup>. d) The N dependence of the  $J/\Psi/D\bar{D}$  ratio can be interpreted as the  $J/\Psi$  being formed through  $c, \bar{c}$  coalescence<sup>10</sup>.

e) Finally, the enhancement factors of hadrons with u,d,s,c quarks may be connected in a simple way to the mass gain of these particles in the quark gluon plasma (table below)<sup>16</sup>.  $T_q$  are the enhancement factors of the lightest mesons with u,d,s,c quarks ( $\pi, K, D$ ), if they are produced out of a quark gluon plasma (e.g.  $g + g \rightarrow s + \bar{s}$  (1)), as compared to their direct production from hadron interactions away from the transition point (e.g.  $p + p \rightarrow K^+ + \Lambda + p$  (2)). The gain is taken proportional to  $m_{particle} - m_{quarks}$ , as this expresses the different thresholds of reactions (1) and (2). In the table below the predicted enhancement factors ( $T_q$ ) of hadrons with u,d,s,c quarks from a QGP are compared to the experimentally measured ones ( $E_q$ ), and are found to be similar. (Definitions:  $th_q = m_0 - m_q$ ,  $m_{u,d} = 7$  MeV,  $m_s = 175$  MeV,  $m_c = 1.25$  GeV,  $m_0 = m(\pi, K, D)$ ,  $T_q = \sqrt{th_q/th_{u,d}}$ ,  $E = \frac{(A+B)}{(N+N)}$ ,  $E_q = E/E_{u,d}$ ).

**Acknowledgments** I would like to thank

| $q$ | $th_q$ | $T_q$ | $E$               | $E_q$ |
|-----|--------|-------|-------------------|-------|
| u,d | 133    | 1     | $\pi/N \sim 1.12$ | 1     |
| s   | 320    | 1.55  | $K/N \sim 2$      | 1.79  |
| c   | 615    | 2.15  | $D\bar{D} \sim 3$ | 2.68  |

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